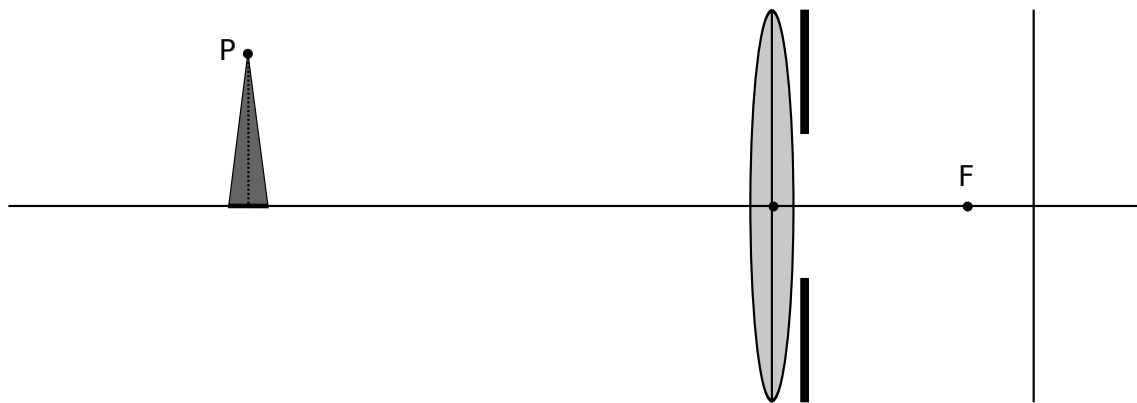




Assignment 2

Welcome to the second assignment of the lecture *Visual Computing* in summer term 2020. **Please read all instructions carefully!** The goal of this exercise is to familiarize you with the mathematical description of *cameras* and *camera calibration*. Submission is due on Monday, Mai 4th, 2020 at 12.00am. Please submit your solutions via `read.mi.hs-rm.de`.

Aufgabe 1. (1 point) Construct the size of the diameter of the *circle of confusion* created when the point **P** is mapped with the lens, aperture and image plane system shown below.



Aufgabe 2. (1 point) The sensor of a camera has a resolution of 2048×2048 pixels. The pixels are square and have a side length of $5.5\mu\text{m} = 0.0055\text{mm}$. How large must a suitable lens be to fully illuminate the sensor?

Aufgabe 3 (1 point). Given is a CCD camera with focal length $f = 6\text{mm}$. The sensor has 640×480 square pixels with a side length of $5\mu\text{m} = 0,005\text{mm}$. The principal point is $\mathbf{h} = (310, 250)^T$. The optical center of the camera is at $\mathbf{C} = (100, 200, 300)^T$ and the orientation of the camera corresponds to the orientation of the world coordinate system. What is the camera matrix \mathbf{P} ?

Aufgabe 4 (3 points). Given is the camera matrix

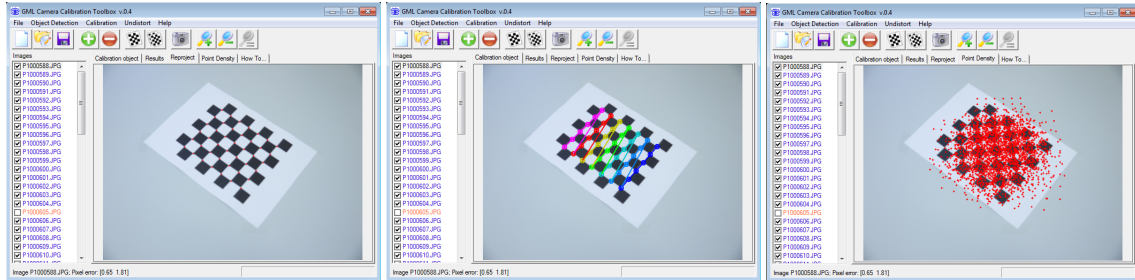
$$\mathbf{P} = \begin{pmatrix} 490 & -390 & -1500 & 1300 \\ -590 & 1400 & -600 & 1300 \\ -0.5\sqrt{2} & -0.3\sqrt{2} & -0.4\sqrt{2} & 5 \end{pmatrix}.$$

Calculate

1. (1 point) the *camera center*,
2. (1 point) the corresponding *calibration matrix* and
3. (1 point) the *orientation* of the camera.



Aufgabe 5 (2 points). Determine the parameters of a camera using the *GML C++ Camera Calibration Toolbox* mentioned in the lecture (see <http://graphics.cs.msu.ru/en/node/909>). You will also find a folder with sample images there.



- (1 point) What are the camera calibration matrix and the coefficients of radial distortion corresponding to the sample images on the website?
- (1 point) Calibrate the camera based on the pictures contained in the archive `calibrationImagesCheckerboard.zip`, which you can find on the website of this lecture. In the archive you will find images of a 7×8 chessboard pattern with $25 \times 25 \text{mm}^2$ in size.

Aufgabe 6 (2 points). Write a simple OpenCV program that rectifies input images using the OpenCV function `undistort` and related calibration parameters – for example, as described in Task 5. In concrete terms, your programme should

- (1 point) import an image together with the associated calibration parameters from a file, and
- (1 point) display the *imported image* as well as the *image that is rectified* using the OpenCV function `undistort`.

The adjacent figures show an example from the data set `calibrationImagesCheckerboard.zip`. Left the (*distorted*) *input image*, right the *same image after rectification*.

